

Julia basics

Using libraries

```
Using libraryname
```

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For example:

```
Using JuMP
```

```
Using Cbc
```

Output

Simplest form:

```
println(expression, expression, expression, ...)
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Any of the `expressions` can be a constant string:

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println("the value of myvariable is: ", myvariable)
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```

C-style output:

Using Printf

```
@printf(format, ...)
```

Conditionals

```
if condition
  ...
elseif condition
  ...
else
  ...
end
```

Loops

```
for i = set
    ...
end
```


Loops

```
for i in set
  ...
end
```

Loops

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for i ∈ set  
  ...  
end
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end
```

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For example `1:5` yields $\{1, 2, 3, 4, 5\}$.

Declaring model variables

With implicit indices

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@variable(model, x[set, set, ...])
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@variable(model, x[i in set, j in set, ... ; condition])
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```
@variable(model, x[i in 1:M, j in 1:N ; i < j])
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Adding bounds directly with variable declaration:

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@variable(model, lb <= x[...] <= ub)
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Example: Lower bound:

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@variable(model, x[i in 1:M] >= 0)
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Adding bounds directly with variable declaration:

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@variable(model, lb <= x[...] <= ub)
```

Example: Lower bound:

```
@variable(model, x[i in 1:M] >= 0)
```

Example: Upper bound:

```
@variable(model, x[i in 1:M] <= 100)
```

Declaring model variables

Adding bounds directly with variable declaration:

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@variable(model, lb <= x[...] <= ub)
```

Example: Lower bound:

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@variable(model, x[i in 1:M] >= 0)
```

Example: Upper bound:

```
@variable(model, x[i in 1:M] <= 100)
```

Example: Lower and upper bounds:

```
@variable(model, 0 <= x[i in 1:M] <= 100)
```

Declaring model variables

Integer variables:

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@variable(model, x[...], Int)
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Binary (i.e. $\{0, 1\}$) variables:

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Integer variables:

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Binary (i.e. $\{0, 1\}$) variables:

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@variable(model, x[...], Bin)
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Example:

```
@variable(model, x[i in 1:M] >= 0, Int)
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Integer variables:

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Binary (i.e. $\{0,1\}$) variables:

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@variable(model, x[...], Bin)
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Example:

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@variable(model, x[i in 1:M] >= 0, Int)
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Note that

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@variable(model, 0 <= x[i in 1:M] <= 1, Int)
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Declaring model variables

Integer variables:

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Binary (i.e. $\{0, 1\}$) variables:

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Example:

```
@variable(model, x[i in 1:M] >= 0, Int)
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Note that

```
@variable(model, 0 <= x[i in 1:M] <= 1, Int)
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is equivalent to

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@variable(model, x[i in 1:M], Bin)
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Declaring model constraints

With a for loop:

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    @constraint(model, expression)
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```

Example:

```
for i in 1:M
    for j in 1:N
        if i < j
            @constraint(model, x[i, j] <= i + j)
        end
    end
end
end
```

Declaring model constraints

All at once:

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@constraint(model, [i in set, ...], expression)
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@constraint(model, [i in set, ...], expression)
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Example:

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@constraint(model, [i in 1:M, j in 1:N ; i < j], x[i, j] <= i + j)
```

Custom sets

So far, all `sets` were `a:b`, but we can have arbitrary sets:

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myset = Set([expression for i in set if condition])
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Example:

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```
Set([2, 4, 6, 8, 10, 12, 14, 16, 18, 20])
```

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Example:

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myset = Set([2 * i for i in 1:10])
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```
Set([18, 4, 14, 10, 20, 2, 16, 8, 6, 12])
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Custom sets

We can also have arbitrary **multidimensional** sets, for example:

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myset = Set([(i, j) for i in 1:3, j in 1:3 if j < i])
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for (i, j) in myset
    println(i, " ", j)
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We can also have arbitrary **multidimensional** sets, for example:

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myset = Set([(i, j) for i in 1:3, j in 1:3 if j < i])
```

which we can use like this:

```
for (i, j) in myset
    println(i, " ", j)
end
```

Output:

```
3 1
3 2
2 1
```

Custom sets

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- ▶ `setdiff(set1, set2, ...)`

Custom sets

The point of using `Set(...)` is that we can do

- ▶ `union(set1, set2, ...)`
- ▶ `intersect(set1, set2, ...)`
- ▶ `setdiff(set1, set2, ...)`

and test for inclusion:

```
if value in set
    ...
end
```

Read the documentation!

<http://www.juliaopt.org/JuMP.jl/v0.19.0/>